

Q. 15. (i) $\frac{u^2 \sin^2 \alpha}{2g} = 3.6 \dots \textcircled{1}$
 $\frac{2u^2 \sin \alpha \cos \alpha}{g} = 19.2 \dots \textcircled{2}$

Dividing $\textcircled{1}$ by $\textcircled{2}$

$$\Rightarrow \frac{\tan \alpha}{4} = \frac{3}{16}$$

$$\Rightarrow \tan \alpha = \frac{3}{4}$$

$$\Rightarrow \sin \alpha = \frac{3}{5}$$

Putting this result into $\textcircled{1}$ gives

$$\frac{u^2 \left(\frac{9}{25}\right)}{19.6} = 3.6$$

$$\Rightarrow u^2 = 196$$

$$\Rightarrow u = 14 \text{ m/s}$$

(ii) $R_{\max} = \frac{u^2}{g}$
 $= \frac{196}{9.8} = 20 \text{ m}$

Q. 16. (i) $30^\circ, 150^\circ$

(ii) $R = \frac{u^2 \sin 2\alpha}{g}$
 $= 40$

$$\Rightarrow \frac{784 \sin 2\alpha}{9.8} = 40$$

$$\Rightarrow \sin 2\alpha = \frac{1}{2}$$

$$\Rightarrow 2\alpha = 30^\circ \text{ OR } 150^\circ$$

$$\Rightarrow \alpha = 15^\circ \text{ OR } 75^\circ$$

Q. 17. $H = \frac{u^2 \sin^2 \alpha}{2g}$

$$\Rightarrow 2.5 = \frac{100 \sin^2 \alpha}{19.6}$$

$$\Rightarrow \sin^2 \alpha = 0.49$$

$$\Rightarrow \sin \alpha = 0.7$$

Q. 18. As in Q. 18(iii), $\alpha = 45^\circ$

$$H = \frac{u^2 \sin^2 45^\circ}{2g}$$

$$= \frac{u^2 \left(\frac{1}{2}\right)}{2g}$$

$$= \frac{u^2}{4g}$$

$$R = \frac{u^2 \sin 2(45^\circ)}{g}$$

$$= \frac{u^2}{g}$$

Therefore, $H : R = 1 : 4$

Q. 19. (i) Let $T =$ time of flight

$$\therefore PT = 60 \dots \textcircled{I} \text{ and } QT - \frac{1}{2}(9.8)T^2 = 0 \dots \textcircled{II}$$

When it is at greatest height

$$v_y^2 = u_y^2 + 2a_y s_y$$

$$0 = Q^2 + 2(-9.8)(5.625)$$

$$\therefore 110.25 = Q^2$$

$$\therefore Q = 10.5$$

Put this into \textcircled{II} : $10.5T - 4.9T^2 = 0$

$$\therefore T = \frac{15}{7}$$

Put this into \textcircled{I} : $P\left(\frac{15}{7}\right) = 60$

$$\therefore P = 28$$

(ii) The greatest distance $= 7 \times \frac{15}{7}$
 $= 15 \text{ m}$