

Q. 10. (i) Let initial velocity = u and let the angle of projection be θ

$$u_x = u \cos \theta \quad u_y = u \sin \theta$$

$$s_x = ut \cos \theta$$

$$s_y = ut \sin \theta - \frac{1}{2}gt^2$$

$$s_x = 27 \text{ and } s_y = 0 \text{ when } t = 3$$

$$\Rightarrow 3u \cos \theta = 27 \quad \text{and} \quad 3u \sin \theta - 44.1 = 0$$

$$\Rightarrow u \cos \theta = 9 \quad \text{Equation 1} \quad \Rightarrow u \sin \theta = 14.7 \quad \text{Equation 2}$$

\Rightarrow Horizontal component of initial velocity = 9

Vertical component of initial velocity = 14.7

(ii) Need to find s_y when $s_x = 5.4$

$$\Rightarrow 9t = 5.4$$

$$\Rightarrow t = 0.6$$

$$s_y = 14.7t - 4.9t^2 \quad \dots \text{ let } t = 0.6$$

$$\begin{aligned} \Rightarrow s_y &= 14.7(0.6) - 4.9(0.6)^2 \\ &= 7.056 \text{ m} \quad \dots \text{ height of wall} \end{aligned}$$

(iii) Need to find v_x and v_y when $t = 0.6$

$$v_x = 9$$

$$\begin{aligned} v_y &= 14.7 - gt \\ &= 14.7 - 9.8(0.6) \\ &= 8.82 \end{aligned}$$

$$\vec{v} = 9\vec{i} + 8.82\vec{j}$$

$$\begin{aligned} \text{Speed} &= |\vec{v}| \\ &= \sqrt{9^2 + 8.82^2} \\ &= 12.6 \text{ m/s} \end{aligned}$$

Q. 11. (i) $s_x = ut$

$$s_y = -\frac{1}{2}gt^2$$

$$s_y = -0.1 \text{ when } s_x = 2$$

$$ut = 2$$

$$\Rightarrow t = \frac{2}{u}$$

$$-\frac{1}{2}gt^2 = -0.1 \quad \dots \text{ let } t = \frac{2}{u}$$

$$\Rightarrow \frac{1}{2}g \left(\frac{4}{u^2} \right) = 0.1$$

$$\Rightarrow \frac{2g}{u^2} = 0.1$$

$$\Rightarrow u^2 = 20g$$

$$\Rightarrow u = \sqrt{20g} \text{ m/s}$$

$$t = \frac{2}{u}$$

$$= \frac{2}{\sqrt{20g}}$$

$$= \frac{1}{7} \text{ s}$$

(ii) $u = \sqrt{20g}$

$$= 14 \text{ m/s}$$

(iii) $v_x = 14$

$$\begin{aligned} v_y &= -gt \\ &= -9.8 \left(\frac{1}{7} \right) \\ &= -1.4 \end{aligned}$$

$$\vec{v} = 14\vec{i} - 1.4\vec{j}$$

$$\begin{aligned} \text{Speed} &= |\vec{v}| = \sqrt{14^2 + (-1.4)^2} \\ &= 14.07 \text{ m/s} \end{aligned}$$