

$$\tan B = \frac{12}{12}$$

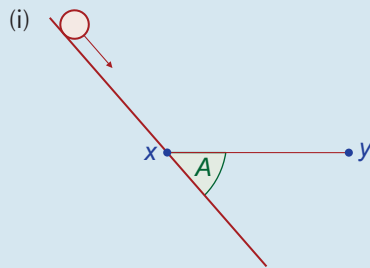
$$\tan B = 1$$

$$\Rightarrow B = 45^\circ$$

$$\begin{aligned} \tan(A + B) &= \pm \frac{\tan A + \tan B}{1 - \tan A \tan B} \\ &= \pm \frac{\frac{4}{3} + 1}{1 - \left(\frac{4}{3}\right)(1)} = \pm 7 \end{aligned}$$

$$\tan(A + B) = -7 \text{ (Since } A + B > 90^\circ \text{)}$$

Q. 14.



$$\tan A = \frac{7}{24}$$

$$\Rightarrow \begin{cases} \cos A = \frac{24}{25} \\ \sin A = \frac{7}{25} \end{cases}$$

$$\begin{aligned} \vec{u} &= 25 \cos A \vec{i} - 25 \sin A \vec{j} \\ &= 24\vec{i} - 7\vec{j} \end{aligned}$$

Before **(Mass)** **After**

$$24\vec{i} - 7\vec{j} \quad 0.1 \quad 24\vec{i} + p\vec{j}$$

$$\frac{\text{NEW}}{\text{OLD}} = -e$$

$$\Rightarrow \frac{p}{-7} = -\frac{3}{7} \Rightarrow p = 3$$

$$\Rightarrow \text{New Velocity} = 24\vec{i} + 3\vec{j}$$

$$\begin{aligned} \text{New Speed} &= \sqrt{24^2 + 3^2} \\ &= 24.2 \text{ m/s} \end{aligned}$$

$$\begin{aligned} \text{(ii) } \vec{I} &= M\vec{V} - M\vec{u} \\ &= 0.1(24\vec{i} + 3\vec{j}) - 0.1(24\vec{i} - 7\vec{j}) \\ &= 1\vec{j} \text{ Ns} \end{aligned}$$

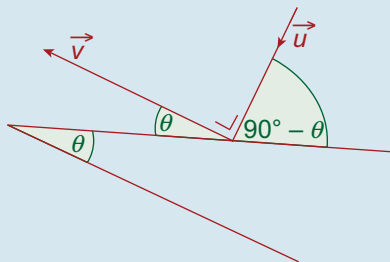
$$\text{Magnitude} = 1 \text{ Ns}$$

$$\begin{aligned} \text{(iii) K.E.}_{\text{before}} &= \frac{1}{2}(0.1)(24^2 + (-7)^2) \\ &= 31.25 \text{ J} \end{aligned}$$

$$\begin{aligned} \text{K.E.}_{\text{after}} &= \frac{1}{2}(0.1)(24^2 + 3^2) \\ &= 29.25 \text{ J} \end{aligned}$$

$$\begin{aligned} \text{Loss} &= 31.25 - 29.25 \\ &= 2 \text{ J} \end{aligned}$$

Q. 15.



$$\vec{u} = -u \cos(90^\circ - \theta)\vec{i} - u \sin(90^\circ - \theta)\vec{j}$$

$$= -u \sin \theta \vec{i} - u \cos \theta \vec{j}$$

$$\vec{v} = -v \cos \theta \vec{i} + v \sin \theta \vec{j}$$

Before

(Mass)

After

$$-u \sin \theta \vec{i} - u \cos \theta \vec{j}$$

M

$$-v \cos \theta \vec{i} + v \sin \theta \vec{j}$$

\vec{i} - velocity is unchanged

$$\Rightarrow -u \sin \theta = -v \cos \theta$$

$$\Rightarrow u \sin \theta = v \cos \theta \quad \dots \text{Equation 1}$$

$$\frac{\text{NEW}}{\text{OLD}} = -e$$

$$\Rightarrow \frac{v \sin \theta}{-u \cos \theta} = \frac{-2}{3}$$

$$\Rightarrow 3v \sin \theta = 2u \cos \theta \dots \text{Equation 2}$$

Dividing 2 by 1 gives:

$$\frac{3v}{u} = \frac{2u}{v}$$

$$\Rightarrow v^2 = \frac{2}{3}u^2$$

$$\Rightarrow \frac{1}{2}Mv^2 = \frac{2}{3}\left(\frac{1}{2}Mu^2\right)$$

$$\Rightarrow \frac{2}{3} \text{ of the energy is preserved.}$$

$$\Rightarrow \frac{1}{3} \text{ of the energy has been lost.}$$