

⇒ Velocity of 1st sphere after impact

$$= u\vec{i} + \frac{6u}{5}\vec{j}$$

⇒ Speed of 1st sphere after impact

$$= \sqrt{u^2 + \left(\frac{6u}{5}\right)^2}$$

$$= \sqrt{u^2 + \frac{36u^2}{25}}$$

$$= \sqrt{\frac{25u^2 + 36u^2}{25}}$$

$$= \sqrt{\frac{61u^2}{25}}$$

$$= \frac{u}{5}\sqrt{61}$$

$$= \frac{\sqrt{61}}{5}u$$

$$q = \frac{1}{5}(5p + 2u) \quad \dots \text{ from Equation 2}$$

$$\Rightarrow q = \frac{1}{5}(5u + 2u)$$

$$\Rightarrow q = \frac{7u}{5}$$

⇒ Velocity of 2nd sphere after impact

$$\frac{7u}{5}\vec{i} + \frac{3u}{5}\vec{j}$$

⇒ Speed of 2nd sphere after impact

$$\sqrt{\left(\frac{7u}{5}\right)^2 + \left(\frac{3u}{5}\right)^2} = \sqrt{\frac{49u^2 + 9u^2}{25}}$$

$$= \sqrt{\frac{58u^2}{25}} = \frac{u}{5}\sqrt{58} = \frac{\sqrt{58}}{5}u$$

(ii) Velocities after impact

$$\text{are } \vec{v}_1 = u\vec{i} + \frac{6u}{5}\vec{j} \text{ and } \vec{v}_2 = \frac{7u}{5}\vec{i} + \frac{3u}{5}\vec{j}$$

$$\text{The slope of } \vec{v}_1 \text{ is given by } m_1 = \frac{\frac{6u}{5}}{u}$$

$$= \frac{6}{5}$$

$$\text{The slope of } \vec{v}_2 \text{ is given by } m_2 = \frac{\frac{3u}{5}}{\frac{7u}{5}} = \frac{3}{7}$$

$$\tan \theta = \pm \frac{m_1 - m_2}{1 + m_1 m_2}$$

$$\Rightarrow \tan \theta = \pm \frac{\frac{6}{5} - \frac{3}{7}}{1 + \frac{18}{35}}$$

$$= \pm \frac{42 - 15}{35 + 18}$$

$$= \pm \frac{27}{53}$$

Take the plus case to find the acute angle

$$\Rightarrow \theta = \tan^{-1} \frac{27}{53} = 27^\circ$$