

$$\Rightarrow 10 \sin A + 10 \mu \cos A = 10 \dots \textcircled{2}$$

Adding equations  $\textcircled{1}$  and  $\textcircled{2}$  we get

$$20 \sin A = 12$$

$$\Rightarrow \sin A = \frac{3}{5}$$

$$\Rightarrow A = \sin^{-1}\left(\frac{3}{5}\right) = 36.87^\circ$$

(ii) From equation  $\textcircled{2}$  we get

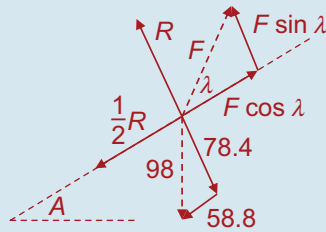
$$10\left(\frac{3}{5}\right) + 10\mu\left(\frac{4}{5}\right) = 10$$

$$\Rightarrow 6 + 8\mu = 10$$

$$\Rightarrow 8\mu = 4$$

$$\Rightarrow \mu = \frac{1}{2}$$

(iii) The force diagram therefore looks like this:



$$R + F \sin \lambda = 78.4$$

$$\Rightarrow R = 78.4 - F \sin \lambda$$

$$\Rightarrow 78.4 - F \sin \lambda = 2F \cos \lambda - 117.6$$

$$\Rightarrow F(2 \cos \lambda + \sin \lambda) = 196$$

$$\Rightarrow F = \frac{196}{2 \cos \lambda + \sin \lambda}$$

$$= 196(2 \cos \lambda + \sin \lambda)^{-1}$$

$$\Rightarrow \frac{dF}{d\lambda} = -196(2 \cos \lambda + \sin \lambda)^{-2} (-2 \sin \lambda + \cos \lambda)$$

$$\Rightarrow \frac{dF}{d\lambda} = \frac{196(\cos \lambda - 2 \sin \lambda)}{(2 \cos \lambda + \sin \lambda)^2}$$

Putting  $\frac{dF}{d\lambda} = 0$  we get

$$\cos \lambda - 2 \sin \lambda = 0$$

$$\Rightarrow 1 - 2 \tan \lambda = 0$$

$$\Rightarrow \tan \lambda = \frac{1}{2}$$

$$\Rightarrow \sin \lambda = \frac{1}{\sqrt{5}} \text{ and } \cos \lambda = \frac{2}{\sqrt{5}}$$

$$F = \frac{196}{2 \cos \lambda + \sin \lambda}$$

$$= \frac{196}{\frac{4}{\sqrt{5}} + \frac{1}{\sqrt{5}}}$$

$$= \frac{196}{\frac{5}{\sqrt{5}}}$$

$$= \frac{196}{\sqrt{5}} \text{ N}$$