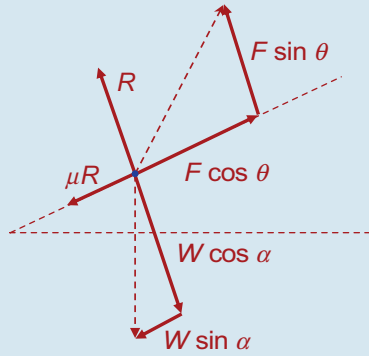


Q. 8. $\mu = \tan \lambda$

The diagram shows resolved forces acting on the particle.



$$R + F \sin \theta = W \cos \alpha$$

$$\Rightarrow R = W \cos \alpha - F \sin \theta$$

$$\mu R + W \sin \alpha = F \cos \theta$$

$$\Rightarrow R \tan \lambda = F \cos \theta - W \sin \alpha$$

$$\Rightarrow R = \frac{F \cos \theta - W \sin \alpha}{\tan \lambda}$$

$$\Rightarrow W \cos \alpha - F \sin \theta = \frac{F \cos \theta - W \sin \alpha}{\tan \lambda}$$

$$\Rightarrow W \cos \alpha - F \sin \theta = (F \cos \theta - W \sin \alpha) \left(\frac{\cos \lambda}{\sin \lambda} \right) \dots \text{multiply by } \sin \lambda$$

$$\Rightarrow W \cos \alpha \sin \lambda - F \sin \theta \sin \lambda = F \cos \theta \cos \lambda - W \sin \alpha \cos \lambda$$

$$\Rightarrow F(\cos \theta \cos \lambda + \sin \theta \sin \lambda) = W(\cos \alpha \sin \lambda + \sin \alpha \cos \lambda)$$

$$\Rightarrow F \cos(\theta - \lambda) = W \sin(\alpha + \lambda)$$

$$\Rightarrow F = \frac{W \sin(\alpha + \lambda)}{\cos(\theta - \lambda)}$$

(i) Force acting up along the plane $\Rightarrow \theta = 0$

$$\Rightarrow F = \frac{W \sin(\alpha + \lambda)}{\cos(-\lambda)} \dots \cos(-\lambda) = \cos \lambda$$

$$\Rightarrow F = \frac{W \sin(\alpha + \lambda)}{\cos \lambda}$$

(ii) Horizontal force $\Rightarrow \theta = -\alpha$

$$\Rightarrow F = \frac{W \sin(\alpha + \lambda)}{\cos(-\alpha - \lambda)}$$

$$= \frac{W \sin(\alpha + \lambda)}{\cos[-(\alpha + \lambda)]}$$

$$= \frac{W \sin(\alpha + \lambda)}{\cos(\alpha + \lambda)}$$

$$= W \tan(\alpha + \lambda)$$

(iii) $F = \frac{W \sin(\alpha + \lambda)}{\cos(\theta - \lambda)}$

Minimum force will occur when $\cos(\theta - \lambda)$ is at its maximum value, i.e. $\cos(\theta - \lambda) = 1$

$$\Rightarrow F_{\text{MIN}} = W \sin(\alpha + \lambda).$$