

$$\sin \alpha = \frac{h}{\frac{u^2}{g\sqrt{3}}} = h \left(\frac{g\sqrt{3}}{u^2} \right)$$

$$\Rightarrow \frac{1}{\sqrt{3}} = h \left(\frac{g\sqrt{3}}{u^2} \right)$$

$$\Rightarrow 3gh = u^2$$

$$\Rightarrow h = \frac{u^2}{3g}$$

Velocity at landing is v_y when $t = \frac{u\sqrt{2}}{g}$

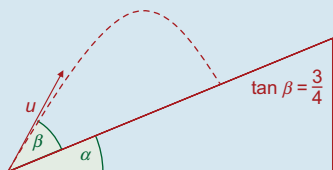
since $v_x = 0$ at landing

$$\Rightarrow v = \frac{u}{\sqrt{3}} - \frac{g\sqrt{2}}{\sqrt{3}} \left[\frac{u\sqrt{2}}{g} \right] = \frac{u}{\sqrt{3}} - \frac{2u}{\sqrt{3}} = -\frac{u}{\sqrt{3}}$$

\Rightarrow Total Energy at landing

$$= \underbrace{\frac{1}{2}m \left[-\frac{u}{\sqrt{3}} \right]^2}_{\text{Kinetic Energy}} + \underbrace{mg \left[\frac{u^2}{3g} \right]}_{\text{Potential Energy}} = \frac{mu^2}{6} + \frac{mu^2}{3} = \frac{1}{2}mu^2$$

Q. 5.



$$\tan \alpha = \frac{3}{4}, \tan \beta = \frac{1}{2},$$

To prove: $\tan \theta = 2$

$$u_x = u \cos \beta$$

$$u_y = u \sin \beta$$

$$a_x = -g \sin \alpha$$

$$a_y = -g \cos \alpha$$

$$\therefore v_x = u \cos \beta - g \sin \alpha t$$

$$v_y = u \sin \beta - g \cos \alpha t$$

$$s_x = u \cos \beta t - \frac{1}{2} g \sin \alpha t^2$$

$$s_y = u \sin \beta t - \frac{1}{2} g \cos \alpha t^2$$

It lands when $s_y = 0$

$$\Rightarrow u \sin \beta t - \frac{1}{2} g \cos \alpha t^2 = 0$$

$$\Rightarrow t = 0 \quad \text{OR} \quad t = \frac{2u \sin \beta}{g \cos \alpha} = \text{time of flight}$$

$$\text{At this time, } v_x = u \cos \beta - g \sin \alpha \left(\frac{2u \sin \beta}{g \cos \alpha} \right)$$

$$= u \cos \beta - 2u \tan \alpha \sin \beta$$

$$v_y = u \sin \beta - g \cos \alpha \left(\frac{2u \sin \beta}{g \cos \alpha} \right) = -u \sin \beta$$

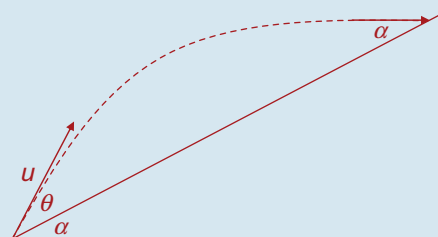
$$\tan \theta = -\frac{v_y}{v_x}$$

$$= \frac{u \sin \beta}{u \cos \beta - 2u \tan \alpha \sin \beta} \quad (\div u \cos \beta)$$

$$= \frac{\tan \beta}{1 - 2 \tan \alpha \tan \beta}$$

$$= \frac{\frac{1}{2}}{1 - 2 \left(\frac{3}{4} \right) \left(\frac{1}{2} \right)} = \frac{\frac{1}{2}}{1 - \frac{3}{4}} = 2 \quad \text{QED.}$$

Q. 6.



$$\tan \alpha = \frac{1}{2} \Rightarrow \cos \alpha = \frac{2}{\sqrt{5}} \text{ and } \sin \alpha = \frac{1}{\sqrt{5}}$$

$$v_x = u \cos \theta - gt \sin \alpha$$

$$= u \cos \theta - \frac{gt}{\sqrt{5}}$$

$$v_y = u \sin \theta - gt \cos \alpha$$

$$= u \sin \theta - \frac{2gt}{\sqrt{5}}$$

$$s_x = ut \cos \theta - \frac{1}{2}gt^2 \sin \alpha$$

$$= ut \cos \theta - \frac{gt^2}{2\sqrt{5}}$$

$$s_y = ut \sin \theta - \frac{1}{2}gt^2 \cos \alpha$$

$$= ut \sin \theta - \frac{gt^2}{\sqrt{5}}$$

For time of flight, let $s_y = 0$

$$\Rightarrow ut \sin \theta - \frac{gt^2}{\sqrt{5}} = 0 \quad \dots \text{ multiply by } \sqrt{5}$$

$$ut\sqrt{5} \sin \theta - gt^2 = 0$$

$$t(u\sqrt{5} \sin \theta - gt) = 0$$