

$$(ii) t_1, \text{ from } Q \text{ to E.P.} = \frac{T}{4} = \frac{2\pi}{4\omega} = \frac{\pi}{2} \text{ s}$$

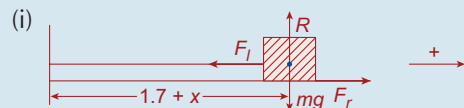
$$t_2, \text{ from E.P. to } P, t_2 = \frac{\text{distance}}{\text{speed}}$$

where  $V = \omega A$  at E.P.

$$\Rightarrow t_2 = \frac{a}{\omega A} = \frac{a}{1(a)} = 1 \text{ s}$$

$$\begin{aligned} \therefore \text{Total time} &= t_1 + t_2 \\ &= \frac{\pi}{2} + 1 \\ &= 2.57 \text{ s} \end{aligned}$$

**Q. 9.**



$$(ii) 1. R = mg = (1)(9.8) = 9.8$$

$$2. F_r = \mu R = \frac{1}{2}(9.8) = 4.9$$

$$3. F_l = k(l - l_0) = 7(1.7 + x - 1) = 4.9 + 7x$$

$$F = F_r - F_l = 4.9 - 4.9 - 7x = -7x$$

$$F = ma$$

$$\Rightarrow -7x = la$$

$$\Rightarrow a = -7x$$

It will perform SHM with  $\omega = \sqrt{7}$ .

$$\text{Periodic time} = \frac{2\pi}{\omega} = \frac{2\pi}{\sqrt{7}}$$

- (iii) The centre of oscillation, where  $x = 0$ , is 1.7 m from  $p$ . It was released where  $x = 2$ . Therefore  $A = 2$ .

It starts from an extreme point

$$\therefore x = A \cos \omega t \Rightarrow x = 2 \cos \sqrt{7}t$$

To find  $t$  when  $x = 0.3$  (i.e.  $2 - 1.7$ )

$$0.3 = 2 \cos \sqrt{7}t$$

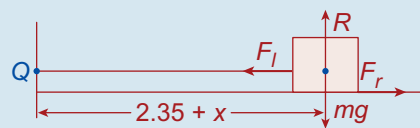
$$\Rightarrow \cos \sqrt{7}t = 0.15$$

$$\Rightarrow \sqrt{7}t = \cos^{-1}(0.15)$$

$$= 1.4202$$

$$\Rightarrow t = \frac{1.4202}{\sqrt{7}} = 0.54 \text{ s}$$

**Q. 10.** (i)



$$1. R = mg = 5(9.8) = 49$$

$$2. F_r = R = (1)(49) = 49$$

$$3. F_l = k(l - l_0) = 140(2.35 + x - 2) = 49 + 140x$$

$$F = F_r - F_l = 49 - 49 - 140x = -140x$$

$$F = ma$$

$$\Rightarrow -140x = 5a$$

$$\Rightarrow a = -28x$$

This is SHM with  $\omega = \sqrt{28} = 2\sqrt{7}$ .

$$(ii) |QO| = 2.35$$

$$(iii) \text{ It starts when } |qp| = 3$$

$$\therefore 2.35 + x = 3$$

$$\Rightarrow x = 0.65$$

The amplitude is, therefore, 0.65

$$(iv) T = \frac{2\pi}{\omega} = \frac{2\pi}{\sqrt{7}}$$



The journey from A to B can be divided into two parts: A to O and O to B.

$$\begin{aligned} \text{A to O: } \frac{1}{4} \text{ of a full cycle } t &= \frac{1}{4} \left( \frac{2\pi}{\sqrt{7}} \right) \\ &= 0.2968 \end{aligned}$$

O to B:  $x = A \sin \omega t$  (starts at centre)

$$0.35 = 0.65 \sin 2\sqrt{7}t$$

$$\Rightarrow \sin 2\sqrt{7}t = \frac{35}{65} = \frac{7}{13} = 0.5385$$

$$\Rightarrow 2\sqrt{7}t = \sin^{-1}(0.5385) = 0.5687$$

$$\Rightarrow t = 0.1075$$

$$\text{Total time} = 0.2968 + 0.1075$$

$$= 0.4043$$

$$= 0.404 \text{ s}$$